

# Shape effects in E2 transition rates from $Z \approx 76$ high-spin isomers

- historical introduction
- structural changes along the yrast line
- K isomerism
- K-forbidden transition rates
- $N_p N_n$  dependence

*Phil Walker*



**Isomer prediction:** Soddy, *Nature* 99 (1917) 433

“We can have isotopes with identity of atomic weight, as well as of chemical character, which are different in their stability and mode of breaking up.”

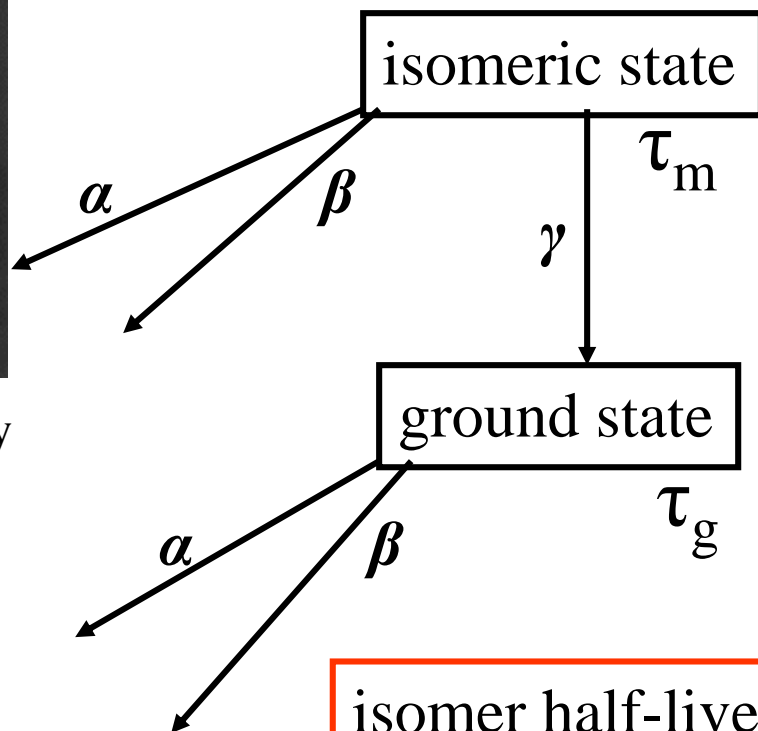
100 years

**explanation:**

von Weizsäcker,  
*Naturwissenschaften*  
24 (1936) 813



Frederick Soddy



spin doctor at age 24



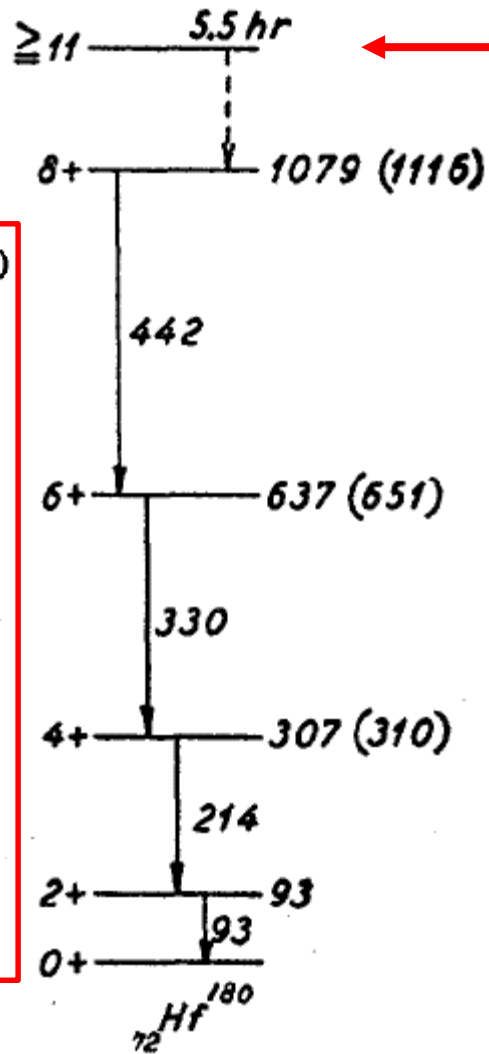
Carl von Weizsäcker

importance  
of  
spin

isomer half-lives range  
from  $10^{-9}$  seconds  
to  $>10^{16}$  years



# $^{180}\text{Hf}$ isomer decay: nuclear collective rotation



$I^\pi = 8^-$  : broken-pair excitation  
*K quantum number not yet recognised*

$$E(I) = (\hbar^2/2\mathfrak{I}) I(I+1)$$

$$\mathfrak{I} \sim 1/3 \mathfrak{I}_{rigid} \Rightarrow \text{superfluidity}$$

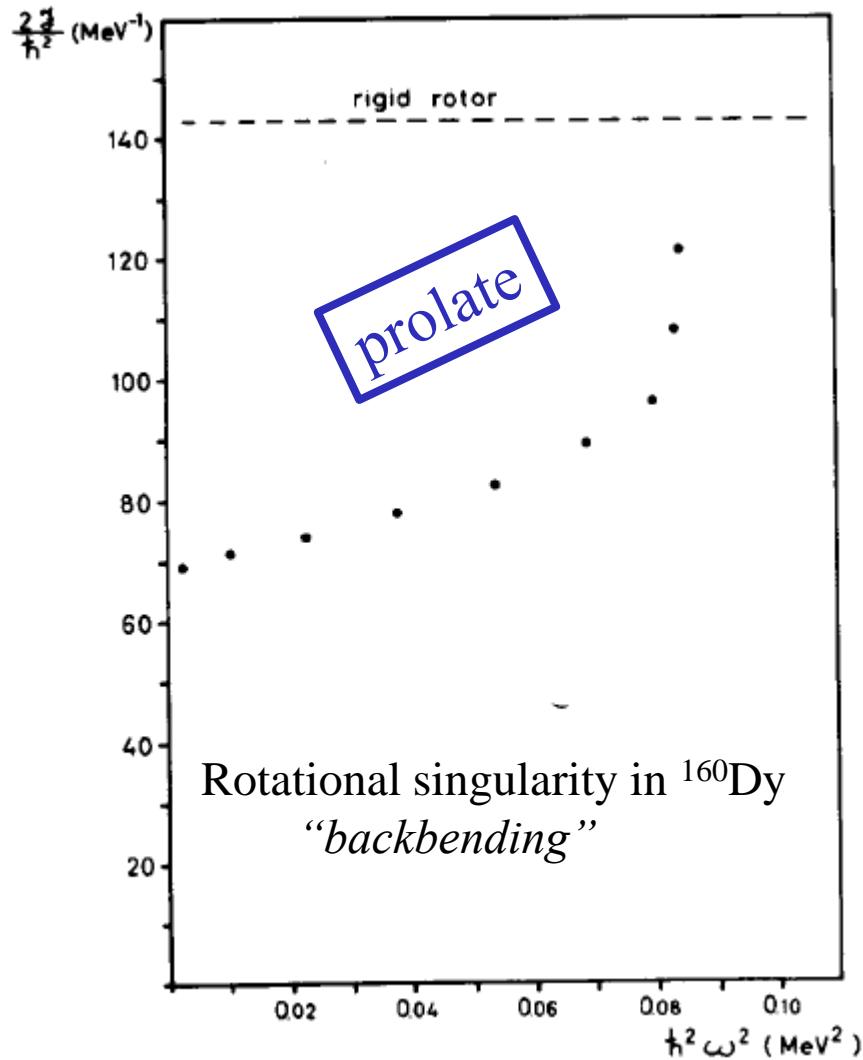
$$^{180}\text{Hf}: E(4+)/E(2+) = 3.30$$

$$\text{perfect rotor}: E(4+)/E(2+) = 3.33$$

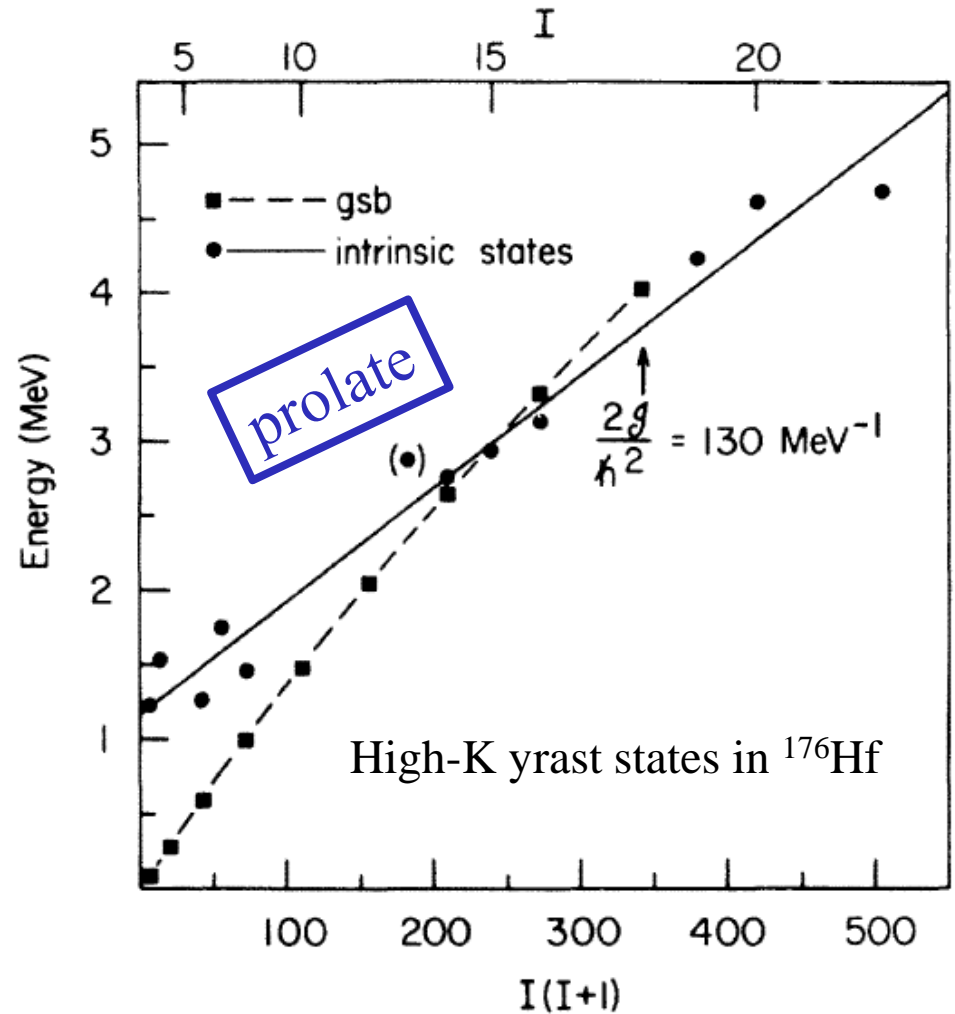
interplay between individual-particle  
 and collective degrees of freedom

structural changes along the yrast line:

rotation alignment in  $^{160}\text{Dy}$ , deformation alignment in  $^{176}\text{Hf}$

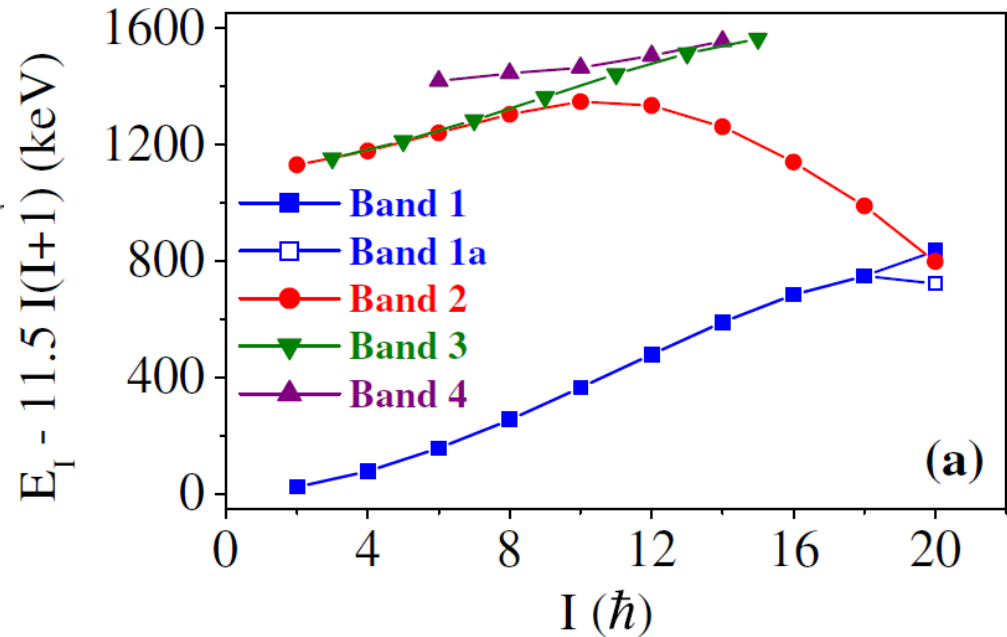
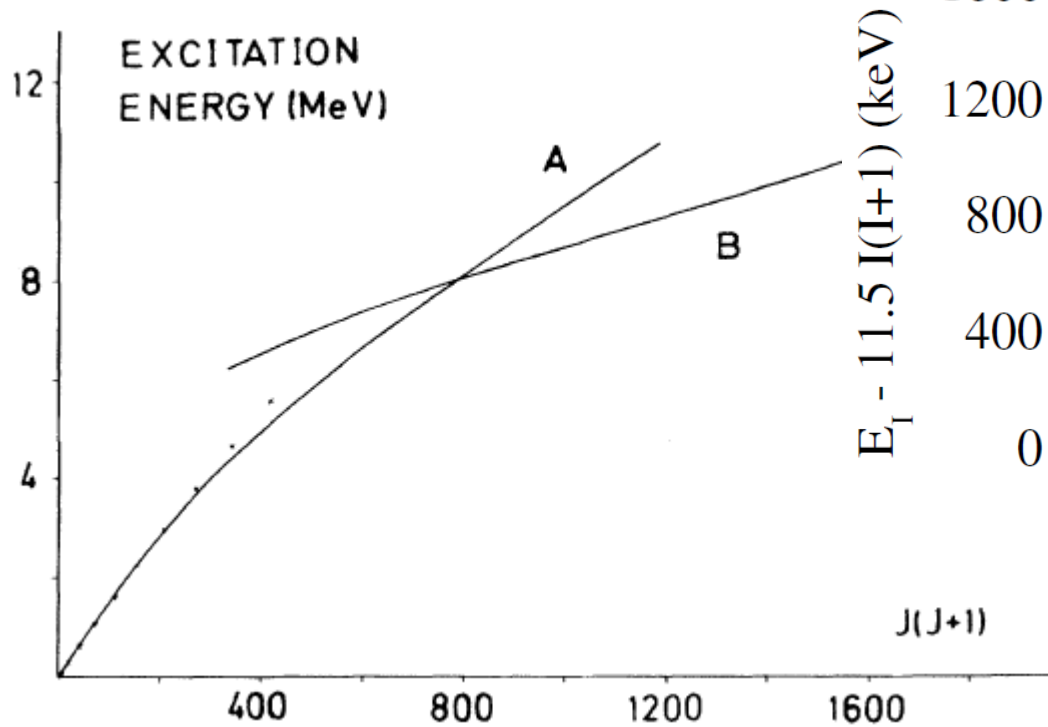


Johnson et al., Phys. Lett. B34 (1971) 605



Khoo et al., Phys. Rev. Lett. 37 (1976) 823

# $^{180}\text{Hf}$ prolate $\rightarrow$ oblate

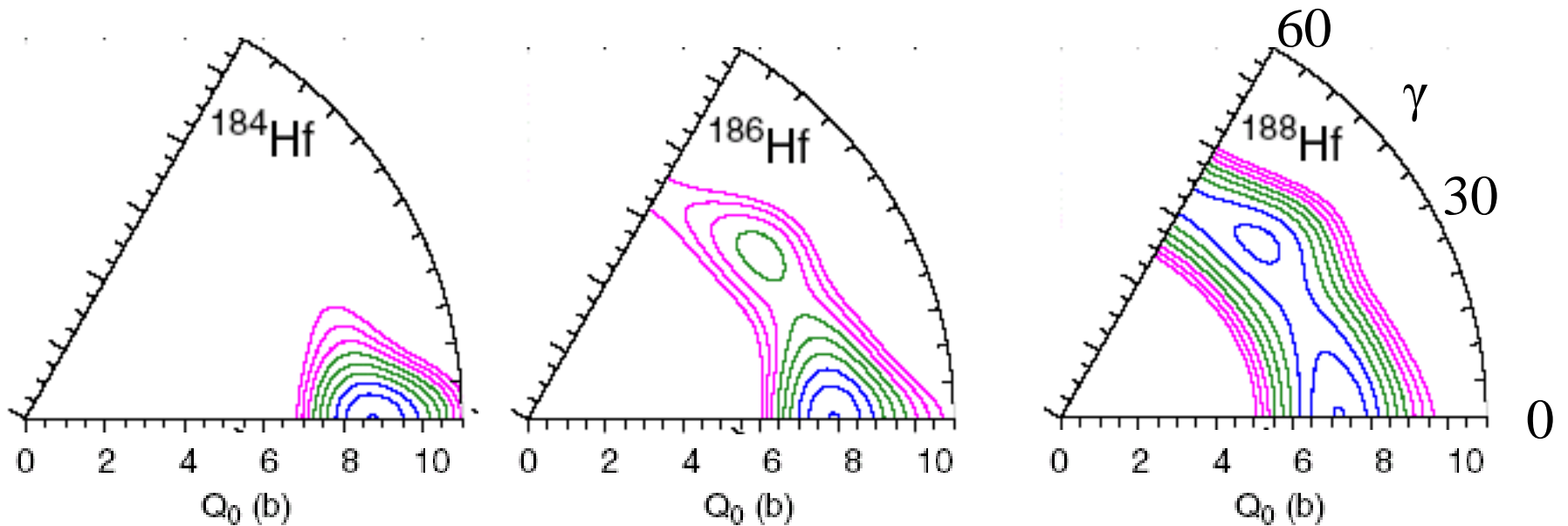


experiment (Gammasphere at ANL):  
Tandel et al. PRL101 (2008) 182503

prediction (HFB):  
Hilton and Mang PRL43 (1979) 1979

prolate  $\rightarrow$  oblate with increasing N

n-rich hafnium ground states (HFB calculations)



N = 112

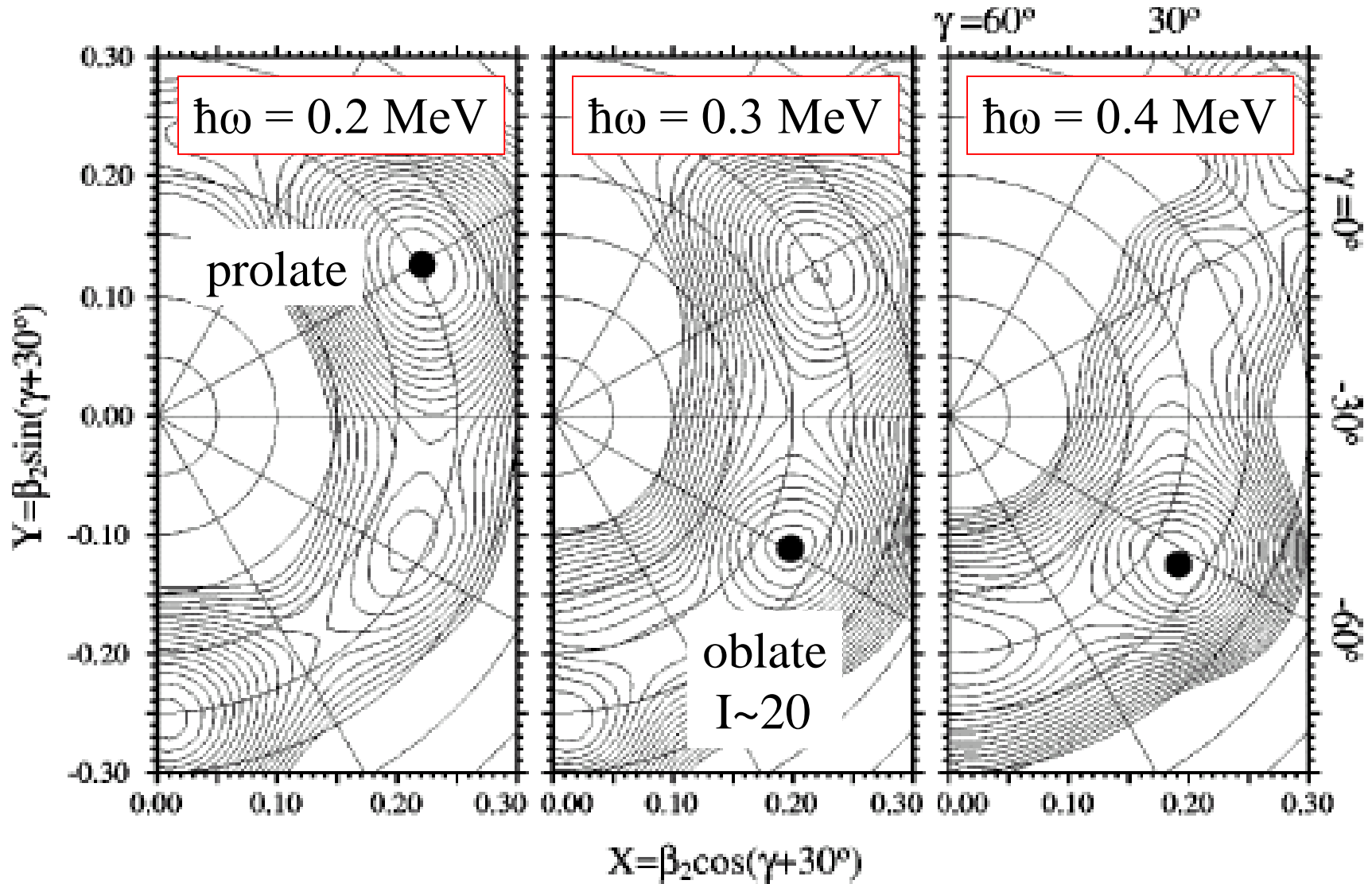
N = 114

N = 116

*Robledo et al., J. Phys. G36, 115104 (2009)*

# total Routhian surfaces (TRS): $^{182}\text{Hf}_{110}$

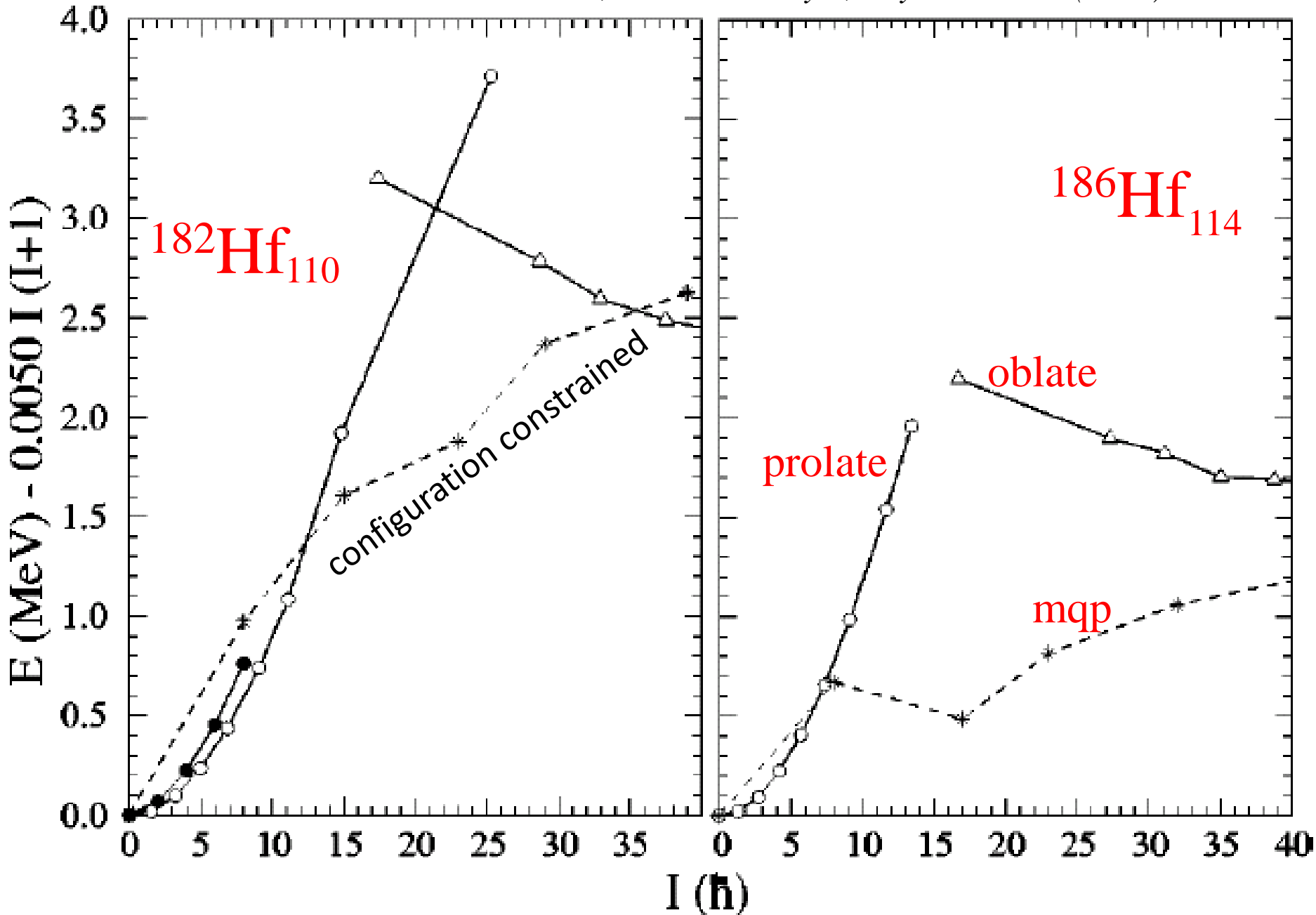
*Xu, Walker and Wyss, Phys. Rev. C62 (2000) 014301*



cf. Hilton and Mang's "giant backbending": PRL43 (1979) 1979

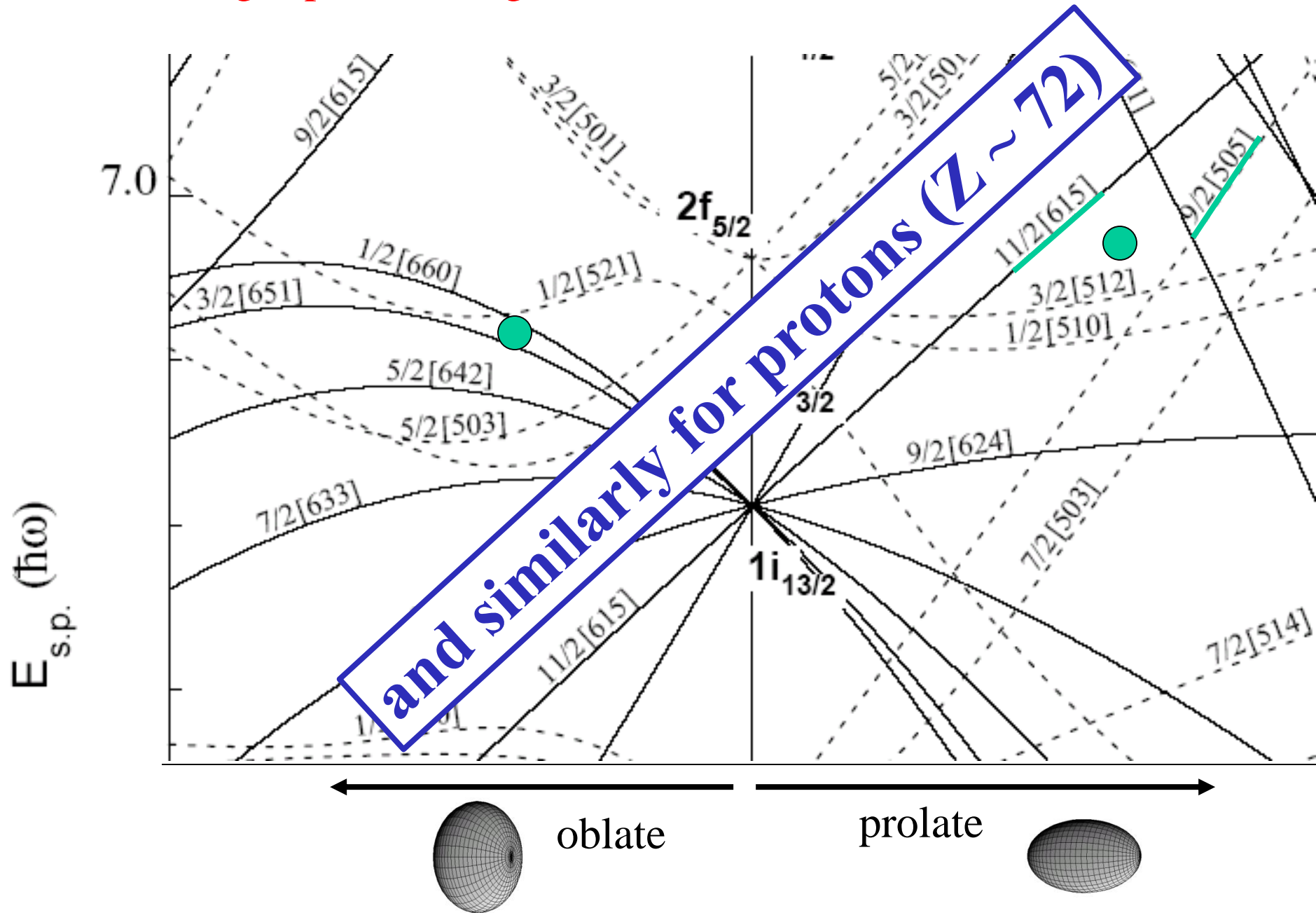
# TRS calculations

*Xu, Walker and Wyss, Phys. Rev. C62 (2000) 014301*

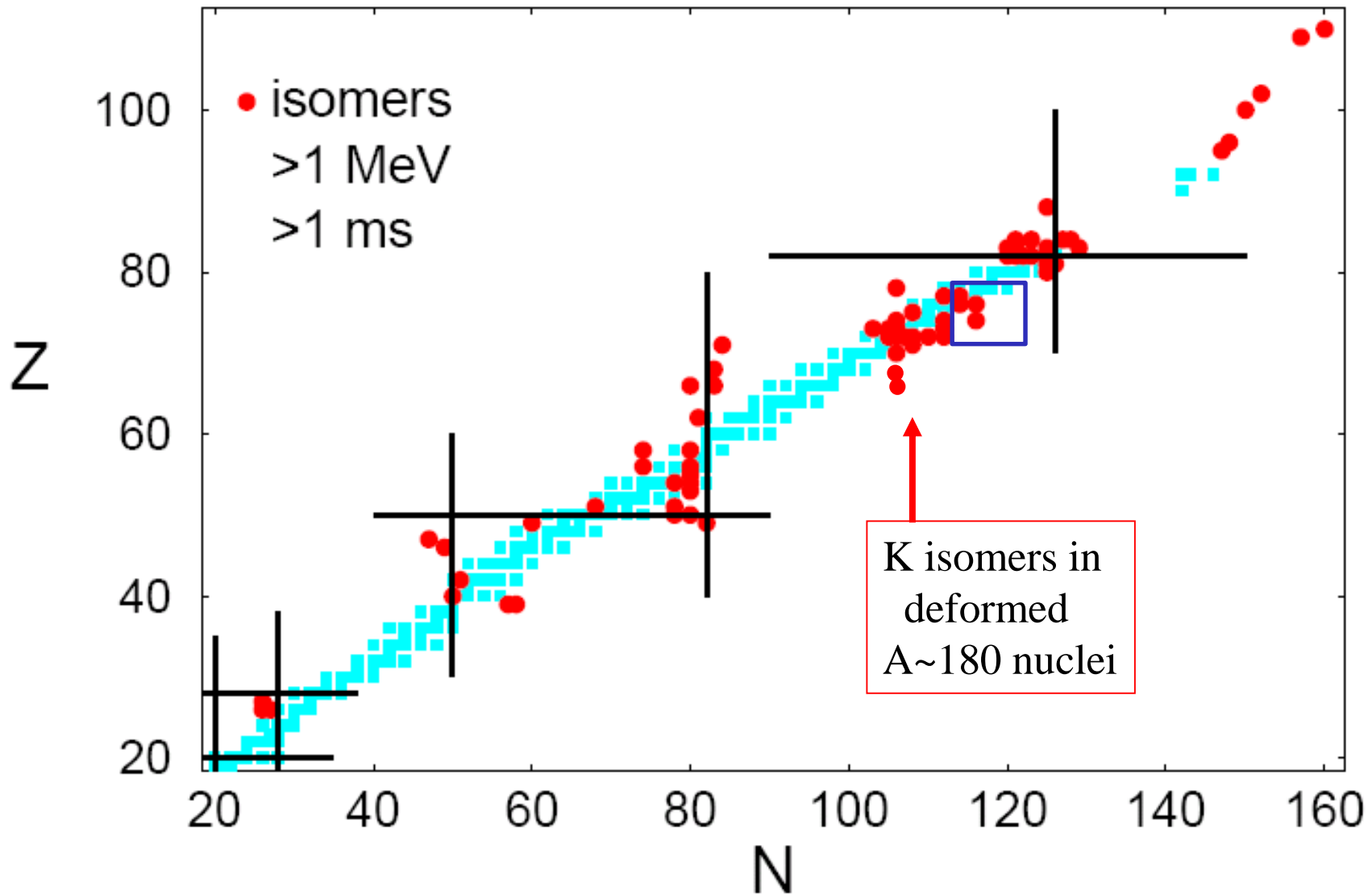




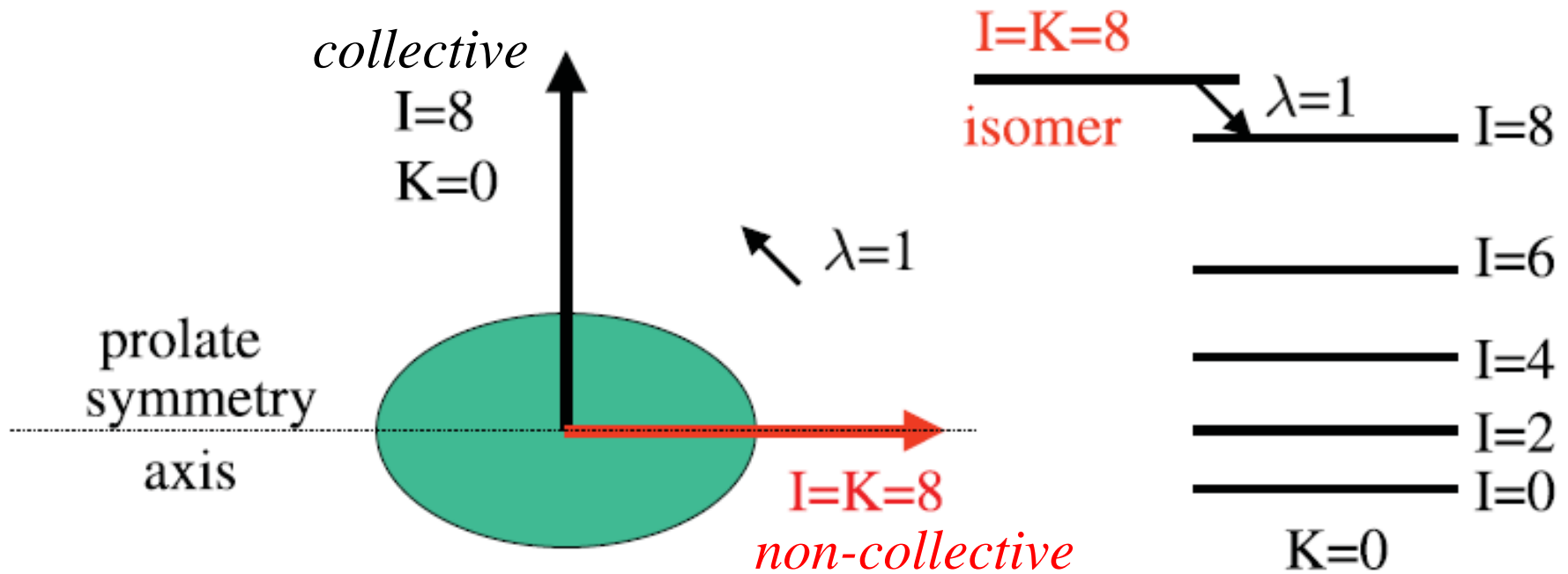
Nilsson single-particle diagram ●  $N = 116$  ( $^{188}\text{Hf}$ ,  $^{190}\text{W}$ ,  $^{192}\text{Os}$ )



# nuclear chart with $>1$ MeV isomers



# K-forbidden $\gamma$ -ray transitions



degree of forbiddenness,  $\nu = \Delta K - \lambda$

$\Rightarrow \lambda=1$  transition is 7-fold K-forbidden ( $\nu = 7$ )

# transition-rate hindrance factors

$$F_W = T_{1/2}^\gamma / T_{1/2}^W$$

*Weisskopf hindrance*

$$\nu = \Delta K - \lambda$$

*degree of K forbiddenness*

$$f_\nu = (F_W)^{1/\nu}$$

*reduced hindrance*  
*(hindrance per degree of K forbiddenness)*

*contains the physics*

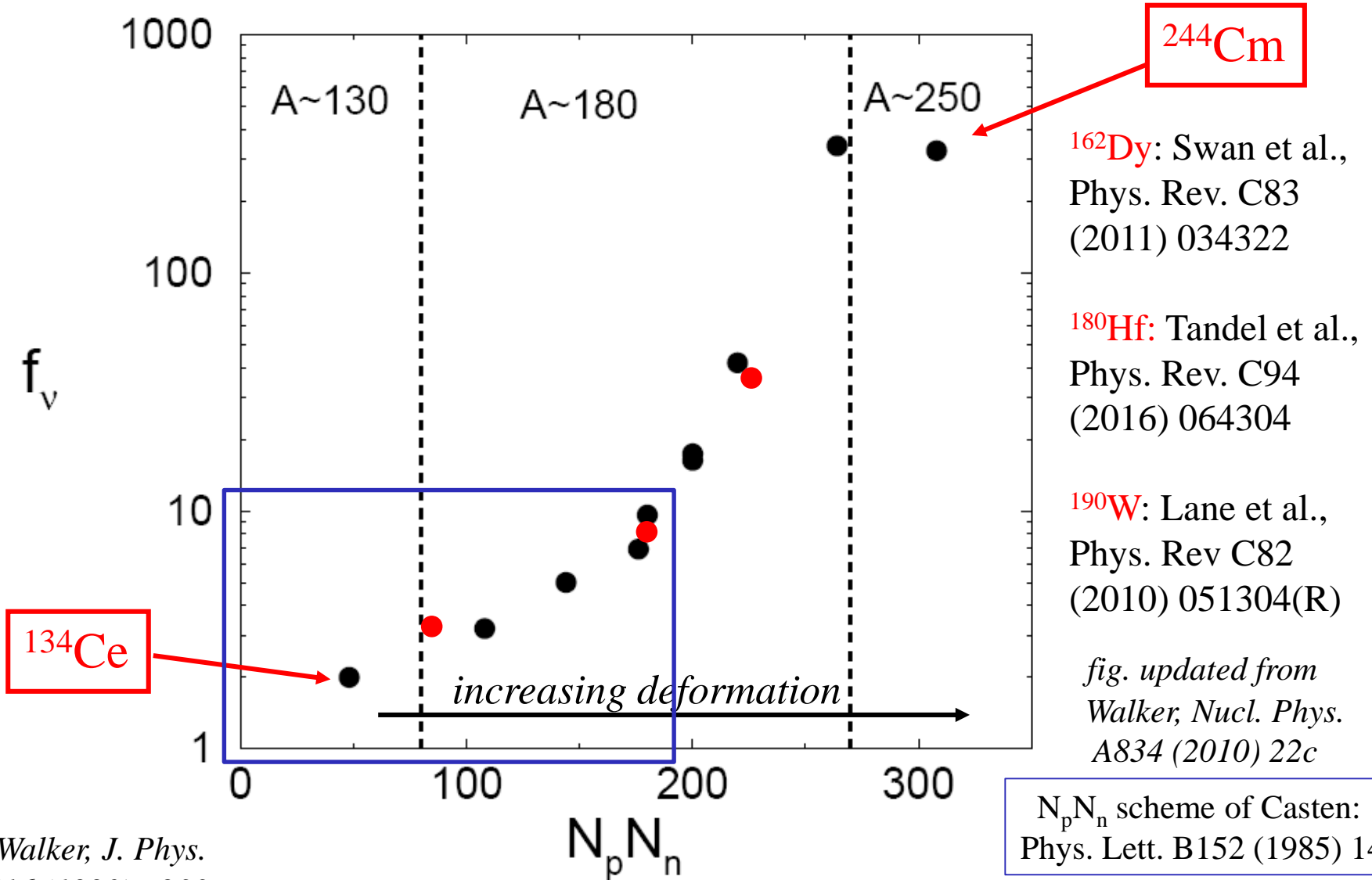
$f_\nu \Leftrightarrow$  broken axial symmetry: rotation (Coriolis)  
non-axial shape ( $\gamma$  deformation)  
random mixing (level density)

in the initial state and/or in the final state

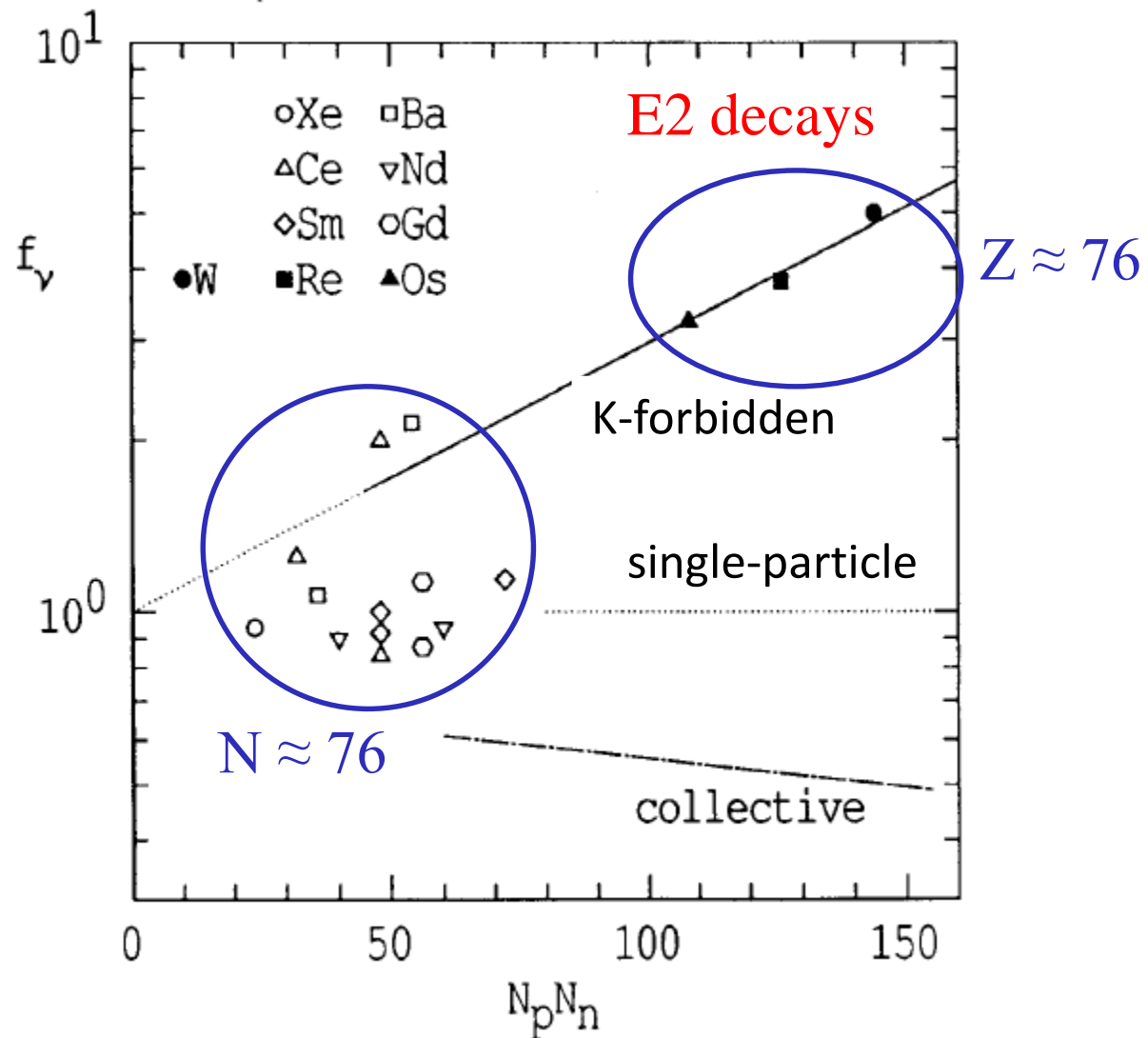
Walker & Xu, Phys. Scr. 91 (2016) 013010; Walker, Phys. Scr. 92 (2017) 054001  
Dracoulis, Walker & Kondev, Rep. Prog. Phys. 79 (2016) 076301

# 2-qp E2 reduced hindrances

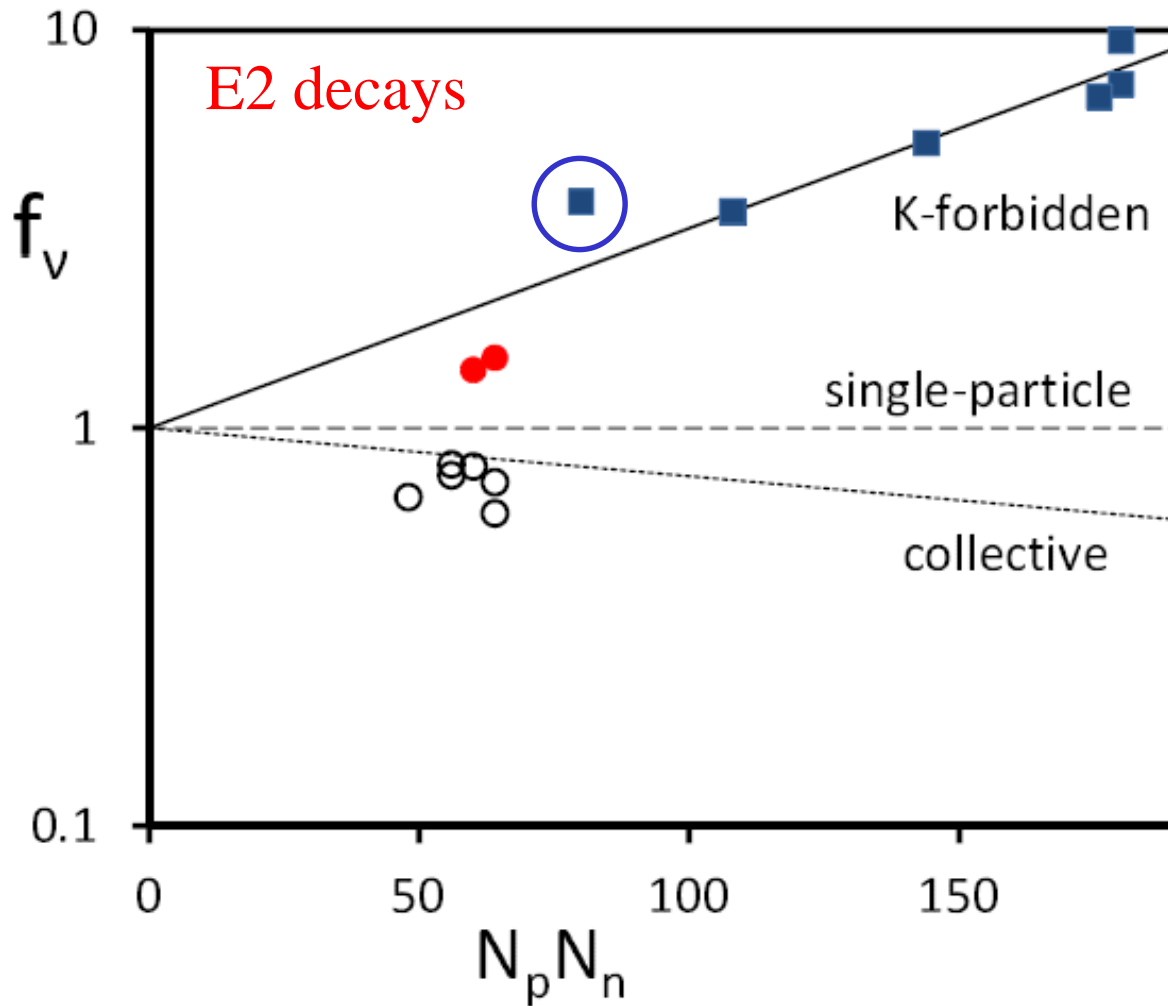
even-even nuclides,  $K^\pi = 6^+, 8^+, 10^+$  isomers

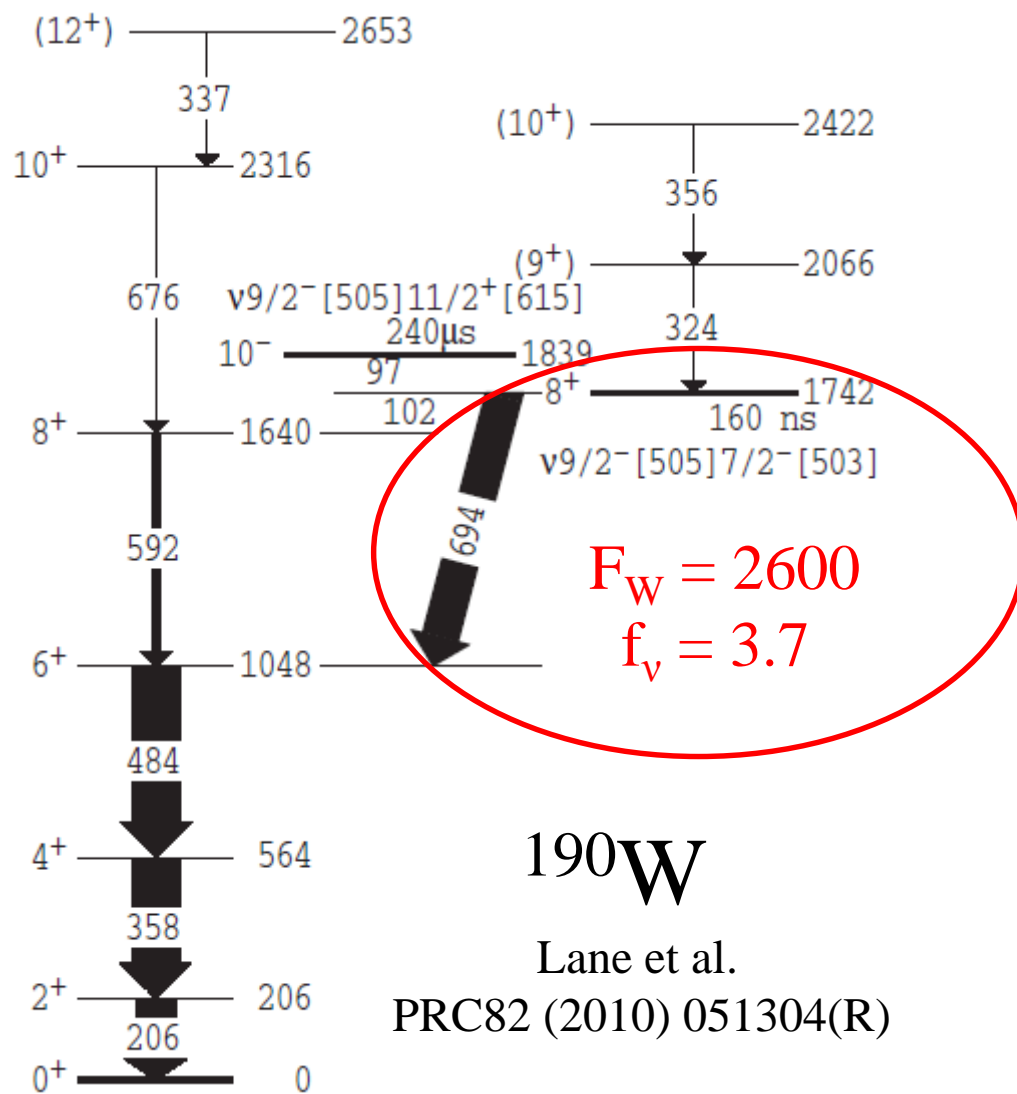


# low $N_p N_n$ values in the $N \approx 76$ region



# low $N_p N_n$ values in the $Z \approx 76$ region

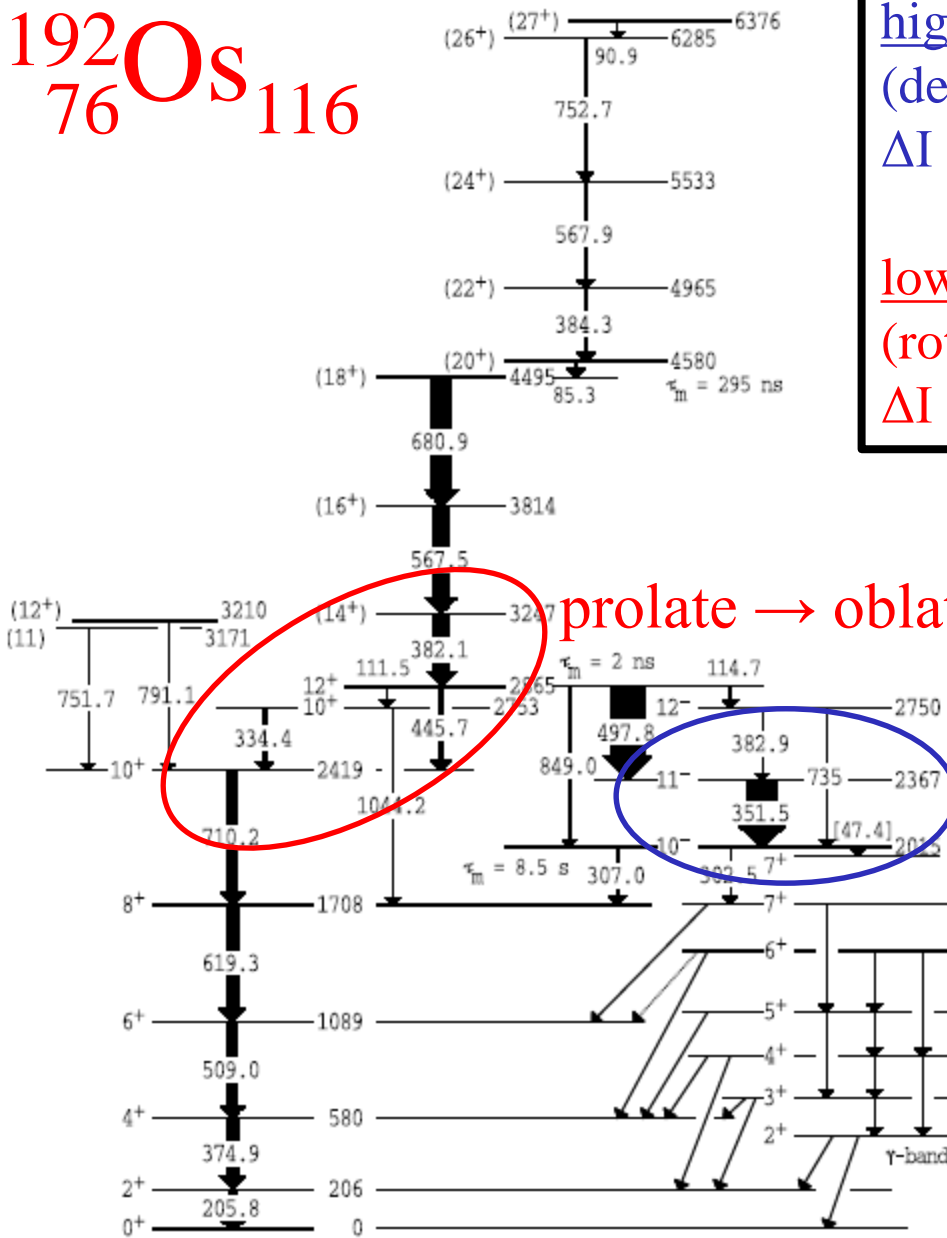






Dracoulis et al. Phys. Lett. B720 (2013) 330  
 (Gammasphere data)

$^{192}_{76}\text{Os}_{116}$



high-K bands:  
 (deformation aligned)  
 $\Delta I = 1$  sequences

low-K bands:  
 (rotation aligned)  
 $\Delta I = 2$  sequences

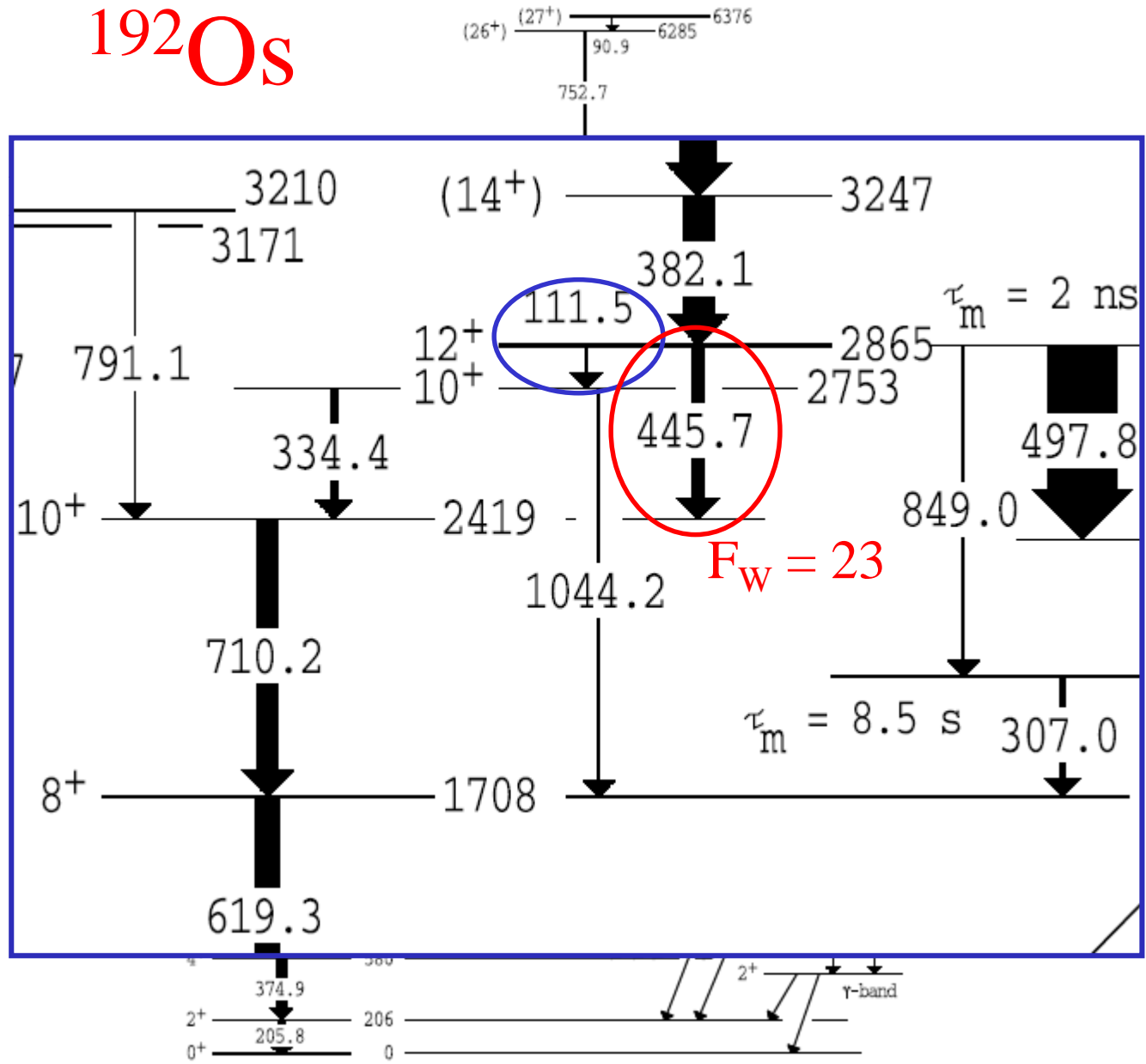
prolate  $\rightarrow$  oblate bandcrossing

high-K

# 192Os

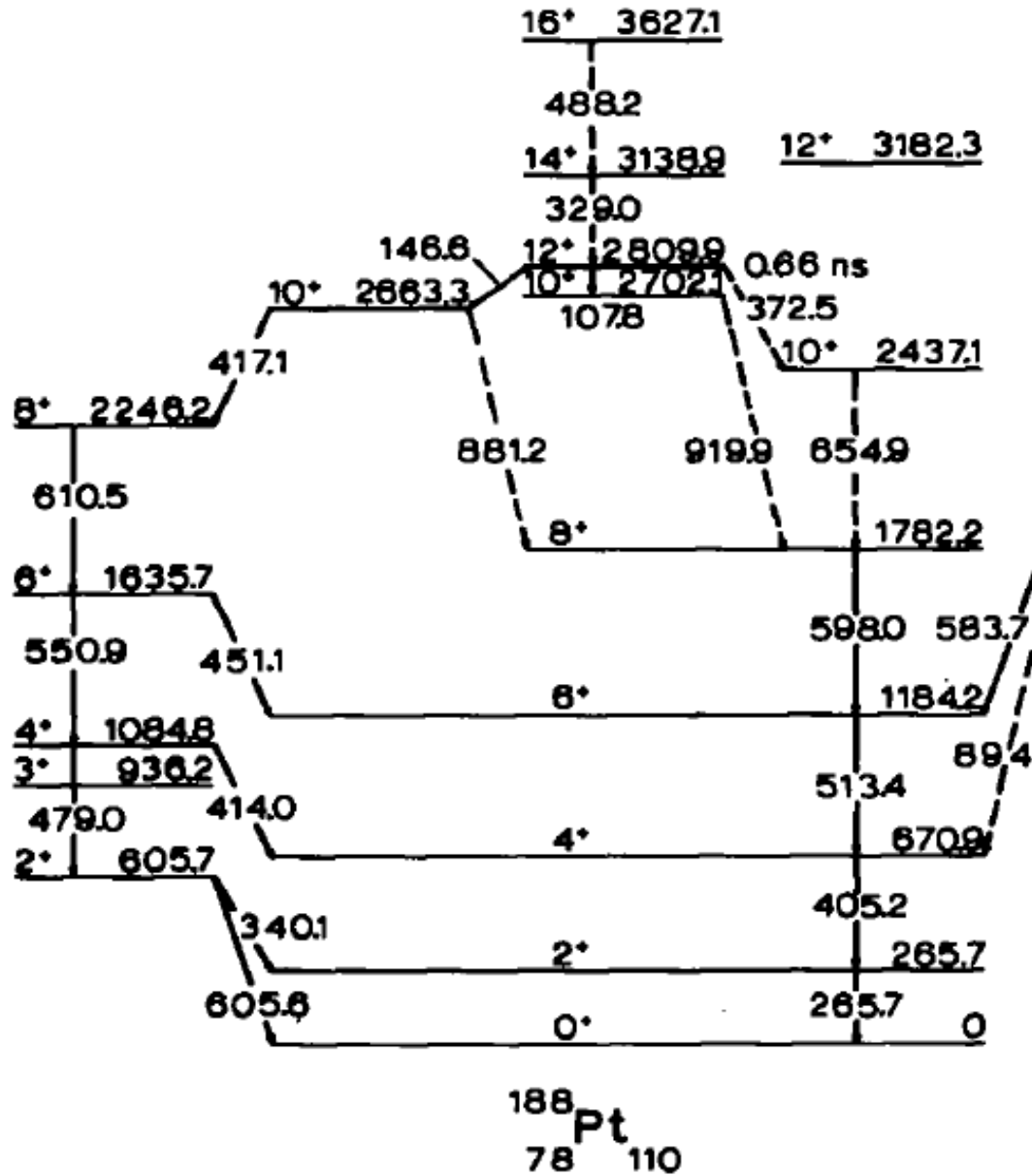
Dracoulis et al. Phys. Lett. B720 (2013) 330

(Gammasphere data)



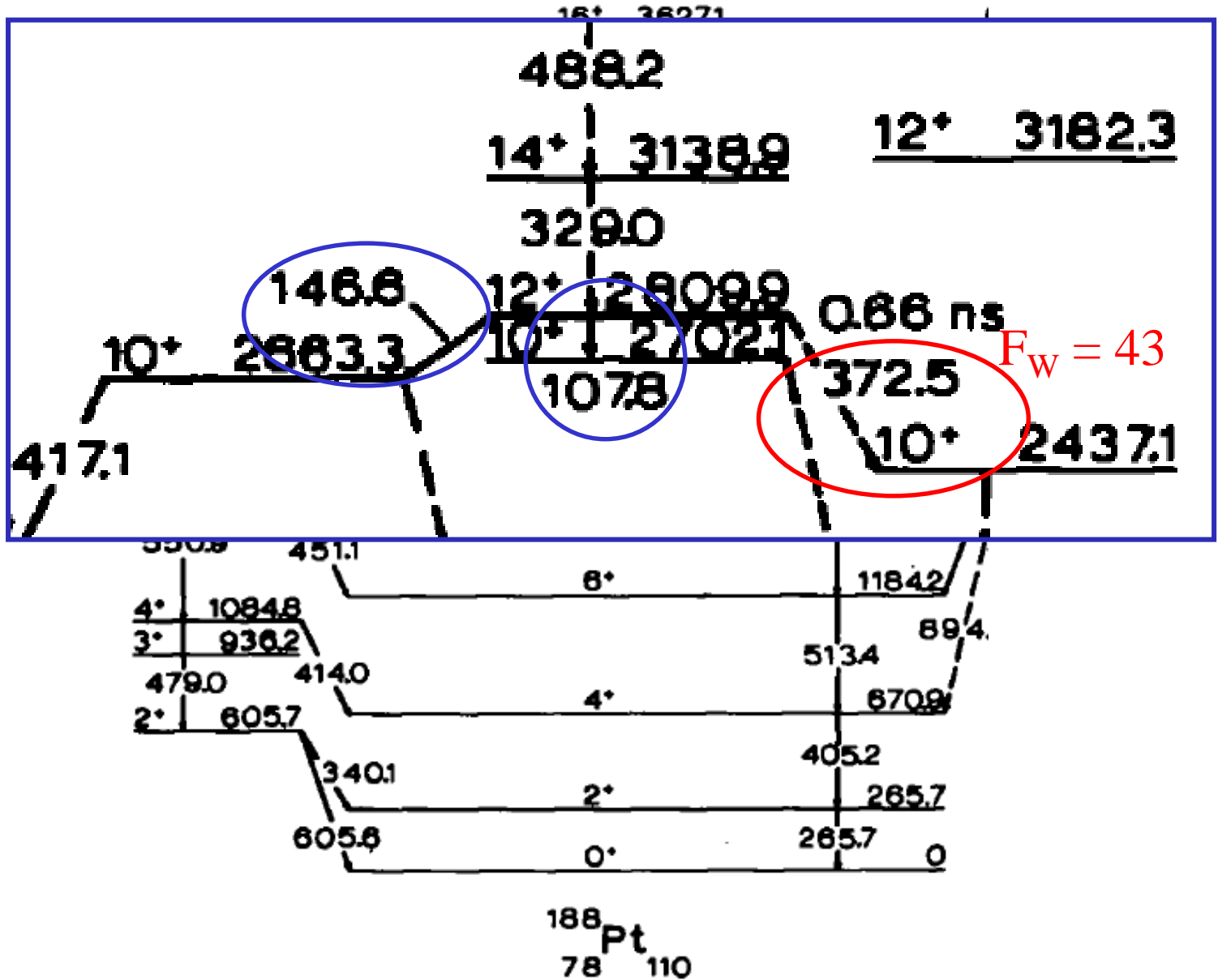
# $^{188}\text{Pt}$

Richter et al., Nucl. Phys. A319 (1979) 221

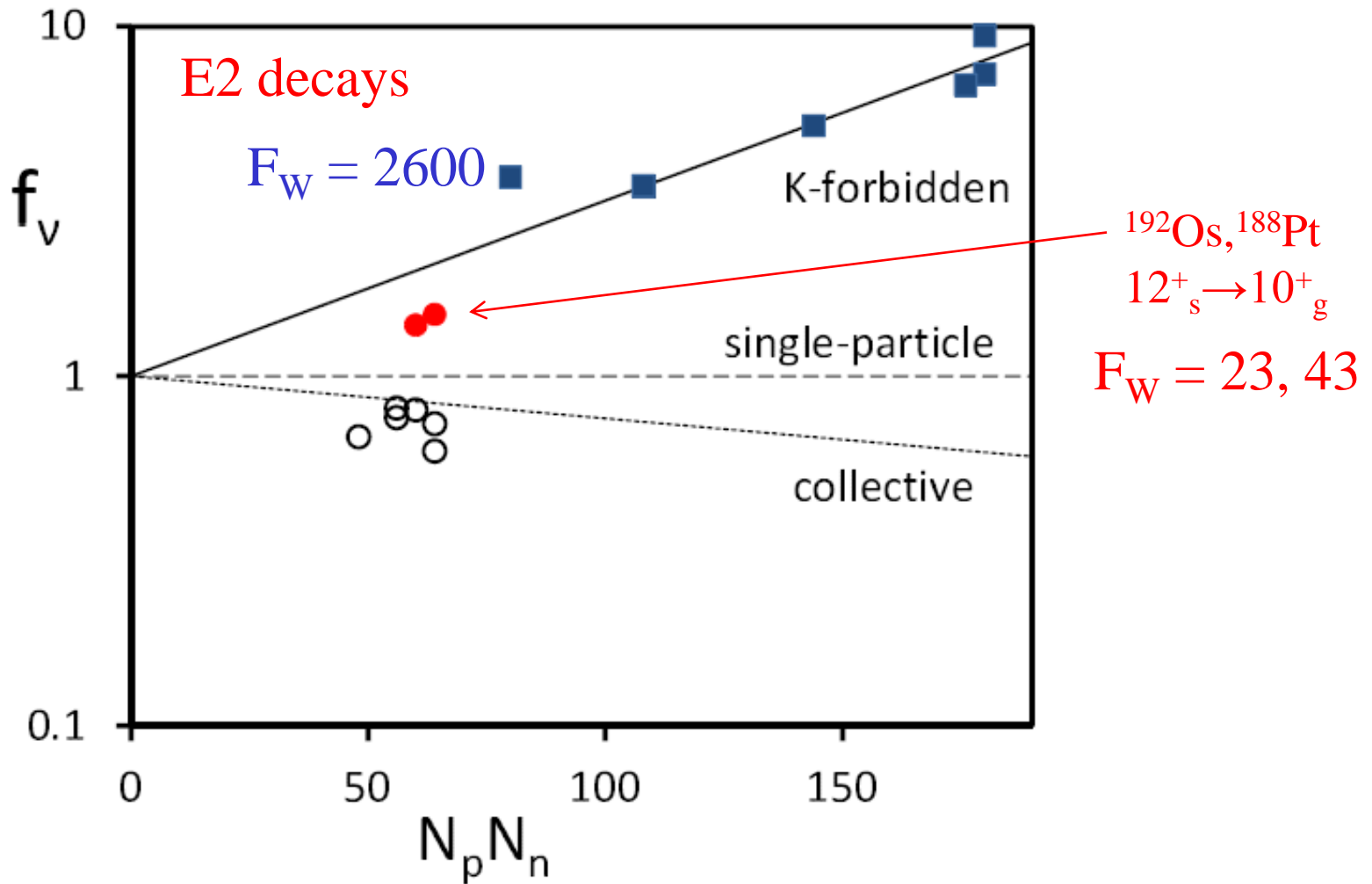


# $^{188}\text{Pt}$

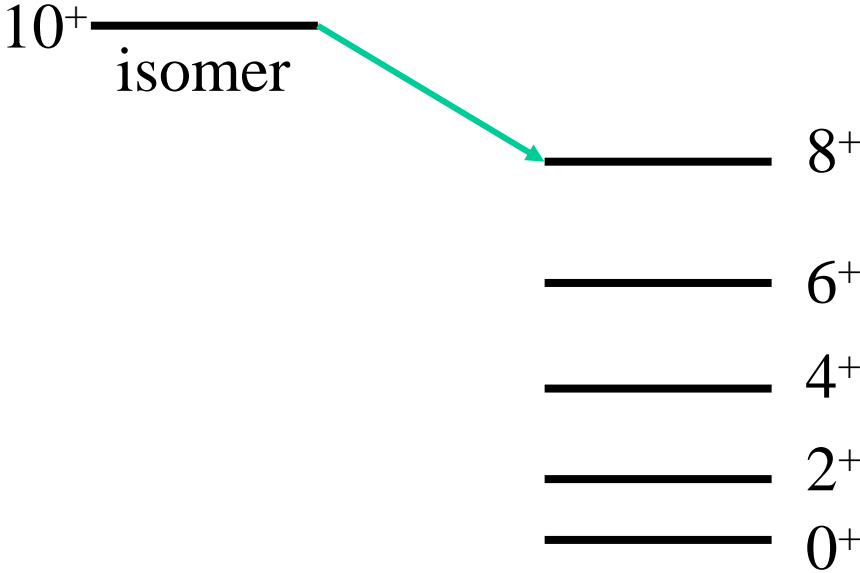
Richter et al., Nucl. Phys. A319 (1979) 221



# low $N_p N_n$ values in the $Z \approx 76$ region



# oblate shape isomer or prolate K isomer?



## Summary:

### n-rich $A \approx 170-190$ region

- E2 reduced hindrance &  $N_p N_n$  dependence
- Different angular-momentum orientations: *K isomers*
- Different shapes: oblate  $\rightarrow$  prolate *shape isomers*
- Examples:  $^{192}\text{Os}$ ,  $^{188}\text{Pt}$  ( $^{190}\text{Pt}$ )
- Future measurements with mass-separated beams

Special thanks to: Furong Xu (Beijing)

Zsolt Podolyák (Surrey)

Filip Kondev (Argonne)

George Dracoulis (ANU)

